

# Lesson 48: Wave Velocity and Boundaries

## Wave Velocity

The speed of a wave does not depend on the **amplitude** or **wavelength** of the wave.

- Instead, the speed of the wave is determined by the properties of the medium it is traveling in.
- Some examples of how the properties of the medium can affect the speed of the wave are:
  1. Speed of water waves depend on the depth of the water.
  2. Speed of waves in a rope depend on the force exerted on the rope and the weight of rope used.
  3. Speed of sound in air depends on the temperature of the air.
- A wave with a bigger **amplitude** does transfer more energy, but it will still travel at the same speed as a smaller **amplitude** wave in that same medium.

## Basic Wave Velocity

If we look at the creation of a single wave pulse, we can determine the velocity of the wave.

- Let's say you are creating a transverse wave pulse in a skipping rope by flicking the end of it with your hand.
- The instant you start to flick your hand upwards, the pulse starts to travel away from you through the rope.
- You will continue to raise your hand until it gets to the highest point (this will be the **amplitude** of the wave), and then your hand starts to come back down.
- By the time your hand gets back to where it started (the equilibrium point), the wave pulse has traveled a certain displacement that is actually the length of the wave pulse.
- Since it traveled this certain length in a certain time, we can determine the velocity of the pulse.

### Warning!

Notice that I said **length**, not **wavelength**. This is because we are only looking at a pulse for now, not a wave train.

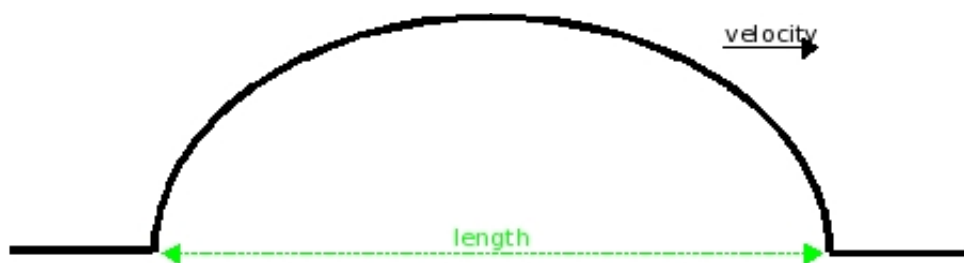


Illustration 1: A pulse, created in a skipping rope, traveling to the right.

$$v = \frac{d}{t} \quad \text{since the displacement traveled is the length...}$$

$$v = \frac{\ell}{t}$$

$v$  = velocity (m/s)

$\ell$  = length (m)

$t$  = time (s)

**Example 1:** It takes you 0.54s to flick your wrist up and down while holding a garden hose. If the pulse you create has a length of 0.78m, **determine** the velocity of the pulse.

$$v = \frac{\ell}{t}$$
$$v = \frac{0.78}{0.54}$$
$$v = 1.4 \text{ m/s}$$

## Universal Wave Equation

Now let's assume that instead of making just a single wave pulse, you continue to flick your hand up and down to create a wave train of crests and troughs.

- Your hand will be flicking up and down with a certain **period** (time to go up and down once).
  - We could take the inverse of the period of your hand to find the **frequency** of your hand's motion.

$$T = \frac{1}{f}$$

- This frequency is also the frequency of the wave you are producing!
- Remember that frequency is measured in Hertz (Hz), which in this case means waves per second.
- We could measure how far the wave has traveled in the entire time it took you to raise and lower your hand one time, and we would find that this is actually the **wavelength** of the wave.
  - Remember that wavelength is just measured in metres.
- Take frequency and wavelength together and you can do a neat little trick.
  - If you multiply them, you are really multiplying cycles/second (frequency) by metres (wavelength), which gives you metres per second (velocity).

$$v = f \lambda$$

$$v = \text{velocity (m/s)}$$
$$f = \text{frequency (Hz)}$$
$$\lambda = \text{wavelength (m)}$$

- This formula is so important, for any kind of wave, that it has been given the name **universal wave equation**.

**Example 2:** A wave in a hot tub is measured to have a frequency of 6.0Hz. If its wavelength is 24cm, **determine** how fast it is moving.

$$v = f \lambda$$
$$v = 60(0.24)$$
$$v = 1.4 \text{ m/s}$$

**Example 3:** The speed of light is always  $3.00 \times 10^8$  m/s. **Determine** the frequency of red light, which has a wavelength of 700nm.

$$v = f \lambda$$
$$f = \frac{v}{\lambda}$$
$$f = \frac{3.00 \times 10^8}{700 \times 10^{-9}}$$
$$f = 4.29 \times 10^{14} \text{ Hz}$$

### Warning!

“Light” is not just the visible stuff that you can see. Radio waves, x-rays, UV, gamma radiation, infrared, microwaves, and more are all forms of light that travel at the same speed. You will learn more about light in Physics 30.

## Waves at Boundaries

Quite often a wave will move from one medium to another, like sound traveling through the air and then into water.

- This may cause the wave to be somewhat distorted (*changed randomly*). We will assume no distortion happens in our examples.
- Moving to a different medium will definitely change the velocity of the wave
- Since the frequency of the source that created the wave remains unchanged, changing the velocity of the wave must result in the wavelength changing as well.

$$v = f \lambda$$

v	varies
f	constant
$\lambda$	varies

To fully explain what happens to the wave, we need to give names to the wave as it goes through changes in media.

- The original wave that was in the first medium = **incident wave**.
- The wave that continues into the new medium = **transmitted wave**.
- Any wave that bounces back = **reflected wave**.

Different things will happen when the incident wave hits the boundary between the two media, depending on the densities of the media compared to each other.

- The two situations we will examine are when the difference in the density of the two media is large, and when the density difference is small.

## Difference in Density is BIG

If there is a big difference between the densities of the media (like a **heavy rope** to a light rope), the following will happen:

1. The **incident** wave will come moving in towards the boundary.



Illustration 2: Incident wave traveling in a heavy rope...

2. When it hits the boundary, almost all of the wave will be **reflected** back the way it came! Almost none of the wave will be **transmitted**.



Illustration 3: ... mostly reflects back into the heavy rope.

- Notice that the **reflected** wave is still right side up (we call this **erect**), and so is the little bit of the **transmitted** wave.
- The reflected wave will be traveling at the same speed, and the transmitted wave will speed up.

This is an example of what happens when the wave is going from **more** to less dense media. A different set of rules apply if it goes from a less to **more** dense media.

- If the wave is going from a less to **more** dense media, then the **reflected** wave is **inverted** (upside down).
- Any part of the wave **transmitted** will still be erect and slow down.

**Example 4:** I hang a giant slinky spring from the ceiling (using very light string). I make a wave travel through the slinky towards the other end, which is just dangling there. **Describe** the waves at the boundary.

The change from the original media (the spring) to the second media (the air) is definitely a BIG change in density, so most of the wave will be **reflected** back through the slinky.

- Since it is going from **more** to less dense, the **reflected** wave will be **erect**.
- The little bit of the wave that is **transmitted** into the air will be **erect** and speed up.

## ***Difference in Density is SMALL***

If the change in density is small, things are a lot easier to remember.

- Quite simply, almost all of the incident wave will be transmitted and stay erect.
- In this example, we use two ropes that have almost the same density, but not quite.



*Illustration 4: Wave pulse traveling through the heavier rope...*

- The incident wave will almost entirely transmit, since there is very little difference for it to even notice.



*Illustration 5: ...transmits to the other, slightly lighter, rope.*

- That's it! The transmitted wave is (almost) the same as the original incident wave.
- Only a very little bit of the wave will be reflected (I didn't even bother drawing it in).